Students Mathematic Problem Solving Process in Two Variable Linear Equation Systems from Cognitive Field Dependent Style

Nuraida
Mathematics Education, IKIP Siliwangi, asrafil.raska@gmail.com

Usman Aripin*
Mathematics Education, IKIP Siliwangi, usmanaripin@gmail.com

Jerito Pereira
Mathematics and Statistics, Guangxi Normal University China, pererla@stu.gxnu.edu.cn

ABSTRACT
This study aims to describe the process of solving mathematical problems in the subjects of a two-variable linear equation system in terms of field-dependent cognitive style. The type of research used is descriptive qualitative research. The research subjects were 15 grade VIII students in one of the public junior high schools in Cimahi City. In this study, the instrument used was a problem-solving test consisting of 2 questions on the material of a two-variable linear equation system and interviews for 3 students with field dependent cognitive style. The results showed that the steps of solving mathematical problems of students with cognitive style field dependent were categorized as good at the stage of understanding the problem and re-examining, categorized enough at the stage of planning completion, and categorized less at the stage of implementing the completion plan. This means, if field dependent students can understand the problem or problem, it will affect the next step.

Keywords: Mathematical Problem Solving Skill, Two-Variable Linear Equation System, Field Dependent Cognitive Style

INTRODUCTION
Etymologically, mathematics comes from the Ancient Greek máthēma which means knowledge, knowledge, and learning(Jha et al., 2016; Machaba & Dhlamini, 2021). Mathematics is one of the sciences that plays an important role(Pereira, J.; Wijaya, T.T.; Zhou, 2020). In addition to
practicing arithmetic and logical thinking skills, the benefits of mathematics are none other than to simplify and help solve problems in everyday life. The purpose of learning mathematics is to develop problem-solving skills.

Solving skill cannot be separated from mathematics learning (Hasbullah & Wibawa, 2021; Ibrahim et al., 2021; Nursha, G., Mirza, A., 2017; Widodo et al., 2021). Polya (1973) suggests that problem-solving is an attempt to find a way out of a goal that is not so easily achievable. In other words, problem-solving is a series of activities in determining the solution to a problem. Polya (1973) also suggested that the solution to the problem-solving problem contains four stages of completion, namely: (1) Understanding The Problem; (2) Devising a Plan (making a problem-solving plan); (3) Carrying Out The Plan (implementing the problem-solving plans); and (4) Looking Back (looking back at the completeness of the problem solving) (Chadli et al., 2019; Gravemeijer et al., 2017; Turyanto et al., 2019).

Problem-solving skills are very important for students because (1) problem solving is a general goal of teaching mathematics, (2) mathematical problem solving includes methods, procedures, and strategies which are the core and main processes in the mathematics curriculum, even as the heart of it. mathematics, and (3) problem solving is a basic skill of mathematics. So it cannot be denied that problem-solving skills are very important both in the learning process and in everyday life. Because problem-solving is a student's first step in developing mathematical skills (Asmar & Hafiz, 2020; Widodo et al., 2018).

In learning activities, of course, students will not be separated from solving mathematical problems that are focused on efforts to train students' mindsets in using their thinking potential (Alifah & Aripin, 2018). Polya (1973) suggests that problem-solving is an attempt to find a way out of a goal that is not so easily achievable. In other words, problem-solving is a series of activities in determining the solution to a problem. Polya (1973) also explained that the solution to problem-solving contains four stages of completion, namely: (1) Understanding the Problem; (2) Devising a Plan; (3) Carrying Out the Plan; and (4) Looking Back (looking back at the completeness of the problem solving).

In the 2013 curriculum, problem-solving is one of the goals in the learning process. Problem-solving in mathematics needs to be learned by students so that they can combine elements of knowledge, techniques, rules, skills, and concepts that have been previously learned to obtain new solutions (Marwazi, Masrakan, & Putra, 2020). Solving mathematical problems becomes meaningful and important to develop students' abilities in understanding mathematical concepts and solving problems (Utomo, Juniati, & Siswo, 2017).

However, from several research results, it was found that the problem-solving skill of high school students was still relatively low, this result was revealed by Purnamasari (2015) showed that students who had problem-solving skills at high qualifications were only 11.77% and students who had low problem-solving abilities and very low as much as 52.94%. Students have difficulty solving problems caused by several things, including students who do not understand the problem given (Wulan & Anggraeni, 2020).

Nahdataeni & Linawati (2015) reveal that the questions that are called problems are questions that cannot be done with a routine process and provide challenges in doing so. For example, when
solving a story problem of non-routine form, the problem is not immediately solved by using a formula that has been taught from school but requires further thought in solving it. Indriyani (2018) also suggests that one form of a question that can hone problem-solving skills is story questions related to everyday life.

On the other hand, there are still many students who have difficulty in solving non-routine story questions. Students difficulties in solving problem-solving problems can be seen from research conducted by Lestari (2010) explaining that one of the errors in solving math story problems consists of conceptual errors and lack of practice in math problems. In addition, students cannot change the question sentence in the mathematical model, so students are confused or wrong when substituting the formula. Widodo (2013) also suggests that students mistakes when making problem-solving plans are that students do not know the adequacy and necessity of the requirements of a problem and do not use all the information that has been collected from the problem.

Vendiagrys & Junaedi (2015) suggested that in solving mathematical problems, students have different abilities. The choice of solutions in solving different mathematical problems can be caused by differences in cognitive styles. Cognitive style is the way a person processes, stores or uses the information to respond to a task or various types of environmental situations (Ngilawajan, 2013). It is referred to as a style and not as a skill because it refers to how a person processes information and solves problems and does not refer to how the process of solving it is best.

Cognitive styles are divided into field dependent (FD), field independent (FI), reflective and impulsive (Azhil, Ernawati, & Lutfianto, 2017) but in this study using a field dependent cognitive style (FD). FD cognitive style is a characteristic of someone who has a tendency to depend on the environment and is also easily influenced by the environment. In carrying out tasks or solving problems, individuals with FD style will work better if given extra instructions or guidance. However, students with FD style tend to receive or process information in general (Rahaju, 2014; Kafiar, 2015).

<table>
<thead>
<tr>
<th>Table 1. Indicators of the Problem Solving Process in terms of Field Dependent Cognitive Style</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Understanding the Problem</strong></td>
</tr>
<tr>
<td>Can write down what is known and ask about the problem, able to identify and explain the information obtained in their language but not yet clear</td>
</tr>
<tr>
<td></td>
</tr>
</tbody>
</table>

(Source: Mawardi, et al., 2020)

Based on the description above, in contrast to the research conducted by Selan & Yuniinta (2017), the focus in this study is to describe the process of mathematical problem-solving abilities.
based on the cognitive style of FD on the material of a two-variable linear equation system. The objectives to be achieved in this research are to find out and explain student profiles in the problem-solving process based on Polya's problem-solving steps. So that the FD style is suitable for use in this study which involves the problem-solving process of each research subject in accordance with the problems often faced by students when encountered in the field, especially in the material of a two-variable linear equation system that is closely related to everyday life. So this is the reason for the authors to choose the FD cognitive style based on Polya's measures to be the focus of this research.

METHOD

This research is qualitative descriptive research. Qualitative descriptive research is a method used to describe and describe existing phenomena, both natural and human-engineered, which pay more attention to the characteristics, quality, and interrelationships between activities (Martin & McKneally, 1998; Mirhosseini, 2017) & Sukmadinata, 2017). According to Herutomo (2014) qualitative descriptive research is research that aims to understand the phenomena experienced by research subjects related to behavior, perceptions, actions, and others, holistically and by means of descriptions of words and language, in a special context that scientific and by utilizing various scientific methods. The phenomenon described in this study is the student's problem-solving process in terms of cognitive style and analyzed using the Polya step, namely at the stage of understanding mathematical problems, planning the stages of problem-solving, implementing the solution plans that have been prepared, and re-examining the answers.

The process of selecting research subjects begins with giving a cognitive style test to class VIII students as many as 15 students using the Group Embedded Figure Test (GEFT) instrument with a score range of 0-18 developed by Witkin et al (1975) which consists of 25 items in the form of pictures that divided into 3 parts. With the criteria that students can answer correctly 0-9 are classified as FD (Basir, 2015; Lusiana, 2017). There were three students with the lowest GEFT test scores in a row, namely student 1 with a score of 8, student 2 with a score of 6, and student 3 with a score of 5.

Then a problem-solving skill test was conducted. The instrument used in this research is a problem-solving skill test compiled by the author in the form of a description of 2 questions. A problem-solving problem contains a situation that can encourage students to solve it but does not directly know-how. This is in accordance with the opinion of Kesan (2010) which states that questions that are included in the problem-solving category are not easy to find a solution to because it requires a process of applying a mathematical mindset and knowledge previously possessed or acquired to new or unusual situations. Guidelines for scoring students' mathematical problem-solving tests are presented in Table 2.

<table>
<thead>
<tr>
<th>Question Number</th>
<th>Problem Solving Steps</th>
<th>Score</th>
<th>Student Response to Problems</th>
</tr>
</thead>
<tbody>
<tr>
<td>1, 2, 3, 4</td>
<td>Step 1. Understanding the Problem</td>
<td>0</td>
<td>No element identification</td>
</tr>
<tr>
<td>Question Number</td>
<td>Problem Solving Steps</td>
<td>Score</td>
<td>Student Response to Problems</td>
</tr>
<tr>
<td>-----------------</td>
<td>----------------------------------------</td>
<td>-------</td>
<td>-------------------------------------------------------------------</td>
</tr>
<tr>
<td>1, 2, 3, 4</td>
<td>Step 2. Devising a Plan</td>
<td>0</td>
<td>There is no mathematical model and problem-solving planning</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2</td>
<td>Mathematical models and problem-solving plans exist but are wrong</td>
</tr>
<tr>
<td></td>
<td></td>
<td>4</td>
<td>Mathematical models and problem-solving plans are incomplete</td>
</tr>
<tr>
<td></td>
<td></td>
<td>7</td>
<td>Mathematical models and planning problem-solving is correct however less complete</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10</td>
<td>Complete and correct mathematical model and problem-solving planning</td>
</tr>
<tr>
<td>1, 2, 3, 4</td>
<td>Step 3. Carrying Out The Plan</td>
<td>0</td>
<td>There is no appropriate calculation problem-solving planning</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2</td>
<td>Calculation according to plan there is a solution to the problem but it's wrong</td>
</tr>
<tr>
<td></td>
<td></td>
<td>6</td>
<td>Calculation according to plan incomplete problem-solving</td>
</tr>
<tr>
<td></td>
<td></td>
<td>9</td>
<td>Calculation according to plan problem-solving is correct but incomplete</td>
</tr>
<tr>
<td></td>
<td></td>
<td>15</td>
<td>Calculation according to plan complete and correct problem-solving</td>
</tr>
<tr>
<td>1, 2, 3, 4</td>
<td>Step 4. Looking Back</td>
<td>0</td>
<td>No conclusion results calculation</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1</td>
<td>The conclusion of the calculation results is there but wrong</td>
</tr>
<tr>
<td></td>
<td></td>
<td>2</td>
<td>The conclusion of the calculation results are complete and correct</td>
</tr>
</tbody>
</table>

(Source: Sari, 2016)

RESULT AND DISCUSSION

The data used is the result of student work on a problem-solving skill test that has a Field Dependent (FD) cognitive style.

1st Process of Students Problem Solving on the System of Linear Equations with Two Variables

At the stage of understanding the problem, based on the results of student answers in Figure 1, student 1 did not rewrite the things that were known and asked in the questions and did not completely state the things that were known and asked in the questions. However, when the interview was conducted, it turned out that student 1 understood the problems contained in the questions.
The stage of understanding the problem can be seen in the results of the interview as follows:

- **P:** What was the first thing you did after receiving the question sheet?
- **S1:** Read the questions carefully and then start working on them.
- **P:** Do you understand the information that is on the question sheet?
- **S1:** Yes I understand.
- **P:** Why don’t you write down what you know and what is asked in the question in your answer?
- **S1:** Because I have understood the matter, ma’am. So write down the answer directly.

At the stage of planning a problem-solving solution, based on the results of student answers in Figure 1, student 1 assumes the things contained in the problem and uses the concept of a two-variable system of linear equations to solve the problem. This can be seen in student 1’s answer, for example by using the variables x and y.

At the stage of implementing the problem-solving plan, based on the results of student answers in Figure 1, student 1 is able to solve the problem according to the plan that has been made and provide conclusions and appropriate answers to solve the problem.

At the re-examination stage, based on the results of student answers in Figure 1, it can be shown that student 1 did a re-examination. The stage of re-examination can be seen from student 1’s answer which concludes in the sentence: “So the price of a notebook is Rp. 3,000 and the price of a pencil are Rp. 2,500” and the sentence “So Lisa’s working hours are 9 hours and Muri’s 7 hours”. By writing conclusions, students have checked what was asked in the question with the results obtained.
2nd Process of Students Problem Solving on the System of Linear Equations with Two Variables

At the stage of understanding the problem, based on the results of student answers in Figure 2, student 2 rewrote the things that were known and asked in the question but did not completely state the things that were known and asked in the question. FD subjects replaced what was known and asked into mathematical sentences, but not all of them were successfully translated, some were still in the form of ordinary verbal sentences (Marwazi, Masrukan, & Putra, 2019).

Figure 2. Answers to Questions by Student 2

The stage of understanding the problem can be seen from interviews with 2 FD students.

P : Do you understand the information in the questions?
S2 : Yes. I wrote down again what was known in the question but it was incomplete.
P : Try to explain what you understand in this matter!
S2 : The command of the question is to determine the price of a pencil and a notebook. And to determine Lisa and Muri's working hours.

At the stage of planning a problem-solving solution, based on the results of students' answers in Figure 2, student 2 assumes the things contained in the problem using the variables x and y, and uses the concept of a system of linear equations with two variables to solve the problem. The plans and actions decided to be used by FD students do not lead to the correct solution, this is because FD students receive information globally so they are less able to organize information independently and use less correct solutions (Haryanti, 2018; Hardianto, 2018). The following are excerpts from interviews with students of 2 FD subjects.

P : To work on this problem, what is the first step you take?
S2 : Write down what is known and make a mathematical model, ma'am.
P : Why did you make a mathematical model first to work on the problem?
S2 : Because to make it easier to do.
At the stage of implementing the problem-solving plan, based on the results of student answers in Figure 2, student 2 is less able to solve the problem according to the plan that has been made and does not provide appropriate conclusions and answers.

At the re-examination stage, based on the results of student answers in Figure 2, it cannot show that student 2 has re-examined. Because student 2 could not find the mistakes made so student 2 could not correct the existing mistakes. This is in line with research (Nugraha, & Zanthy, 2018) which shows that students’ mathematical problem-solving abilities are still low, especially at the stage of re-examining the answers obtained. The following is an excerpt from the results of student interviews with 2 FD subjects.

P : After you solve the problem, do you check the results again?
S2: No.
P : Why don’t you double check your answer?
S2: Because I was sure of my answer.

3rd Process of Students Problem Solving on the System of Linear Equations with Two Variables

At the stage of understanding the problem, based on the results of student answers in Figure 3, student 3 did not rewrite the things that were known and asked in the questions and did not completely state the things that were known and asked in the questions. This is because students with FD style are not guided in doing problem-solving tests, while FD students like to seek guidance and instructions from teachers (Yasa, Sadra & Suweken, 2013).

Figure 3. Answers to Questions by Student 3

At the stage of planning a problem-solving solution, based on the results of students’ answers in Figure 3, student 3 assumes the things contained in the problem using x and y variables, and does
not use the concept of a two-variable linear equation system to solve the problem because it takes a long time to remember the concept of the material. This is in line with the results of previous studies, FD students are not yet complete in developing strategies (Geni, Mastur & Hidayah, 2017).

At the stage of implementing the problem solving plan, based on the results of student answers in Figure 3, student 3 is less able to solve problems according to the plan that has been made and does not provide appropriate conclusions and answers.

At the re-examination stage, based on the results of students' answers in Figure 3, it cannot show that student 3 has re-examined. This is in line with Nurhayati (2013) who said that students ignore Polya's fourth step in solving problems, namely looking back at the complete solution correctly. The re-examination stage can be seen from the results of interviews with students of 3 FD subjects.

\[ P : \text{After you solve the problem, do you check the results again?} \]
\[ S3 : \text{Yes, I checked the answer again.} \]
\[ P : \text{How many times have you checked your answers?} \]
\[ S3 : \text{I checked the answer once.} \]
\[ P : \text{Are you sure about your answer?} \]
\[ S3 : \text{Yes of course.} \]

Table 3. Profile of the Problem Solving Process Subject Student 1, Student 2, and Student 3

<table>
<thead>
<tr>
<th>Polya's Steps</th>
<th>Student Problem Solving Process 1</th>
<th>Student Problem Solving Process 2</th>
<th>Student Problem Solving Process 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Understanding the Problem</td>
<td>Do not rewrite things that are known and asked in written questions. During the interview, student 1 proved to understand the problem</td>
<td>Rewrite the things that are known and asked in the questions but do not completely state the things that are known and asked in the questions</td>
<td>Do not rewrite things that are known and asked in the question</td>
</tr>
<tr>
<td>Devising a Plan</td>
<td>Assume the things contained in the problem by using mathematical symbols and working on the problem according to the concept</td>
<td>Give examples of things in the problem</td>
<td>Suppose the things contained in the problem by using symbols and not using concepts to solve problems</td>
</tr>
<tr>
<td>Carrying Out The Plan</td>
<td>Able to solve problems and provide appropriate conclusions and answers to solve problems</td>
<td>Less able to solve problems and less provide conclusions and appropriate answers</td>
<td>Less able to solve problems and less provide conclusions and appropriate answers</td>
</tr>
<tr>
<td>Looking Back</td>
<td>Make a final conclusion on the answer</td>
<td>Can't prove the answer yet</td>
<td>Check answers that are proven at the interview</td>
</tr>
</tbody>
</table>

From the results of the above analysis, it can be concluded that students with field-dependent cognitive styles have good mathematical problem-solving abilities because they can only achieve several problem-solving steps. At the stage of understanding the problem and re-examining, students with field-dependent cognitive style can be said to be categorized as good enough because they can write down the known data on the problem even though they are still lacking in mentioning the known data. From the results of the interviews, it can be seen that the FD students did a re-examination. At
the stage of planning for completion, it can be said that it is categorized as sufficient because FD students wrote one settlement strategy but there were several steps that were not written. Meanwhile, at the stage of implementing the completion plan, the category is less because FD students can write the completion steps sequentially but it is still not correct because there are concepts used that are not precise and there are errors in calculations.

Thus this is in accordance with research conducted by Haloho (2016) and Syarifuddin (2020) which state that the problem-solving abilities of students with FD cognitive style are categorized as good at the stage of understanding the problem and re-examining, categorized enough at the stage of planning a solution, and categorized as less at the stage of implementing the completion plan. In this study it can be said that if FD students can understand the problem well, then this will affect the next steps.

**CONCLUSION**

Based on the results of the analysis and discussion, it can be concluded that there is a tendency for students to solve problems, students with FD cognitive style are categorized as good at the stage of understanding the problem and re-examining, categorized enough at the stage of planning completion, and categorized less at the stage of implementing the completion plan because students Field dependent cognitive style requires encouragement or more detailed instructions to solve a problem.

This research is expected to provide input for teachers as facilitators who handle students directly to pay attention to students' mathematical problem-solving abilities so that students are accustomed to solving problem-solving problems.

**ACKNOWLEDGEMENT**

The researcher was very aware when the compilers of this article could not complete without the cooperation of various parties. Therefore, on this occasion, the researcher were very grateful to the school, teachers and students who have participated and helped. For all the support from various related parties, we say thank you.

**REFERENCES**


Geni, P. R. L., Mastur, Z., & Hidayah, I. (2017). Kemampuan Pemecahan Masalah Siswa pada...


Students Mathematic Problem Solving Process in Two Variable Linear Equation Systems from Cognitive Field Dependent Style

Nuraida, Usman Aripin, and Jerito Pereira

Pendidikan Matematika Tadulako, 1(1), 115–128.


